



estable courses sometime consiste approximate



OFFICE OF NAVAL RESEARCH

Contract N00014-86-K-0043

R & T Code 413f0001---01

TECHNICAL REPORT No. 27

Role of Coherences in the Relaxation of Adsorbates

bу

Henk F. Arnoldus and Thomas F. George

Prepared for Publication

in

Physical Review B

Departments of Chemistry and Physics State University of New York at Buffalo Buffalo, New York 14260

December 1986

Reproduction in whole or in part is permitted for any purpose of the United States Government.

This document has been approved for public release and sale; its distribution is unlimited.





A1)-	1175	_	773
//UT			//2

REPORT DOCUMENTATION PAGE								
1. REPORT SECURITY CLASSIFICATION Unclassified			1b. RESTRICTIVE MARKINGS					
Za. SECURI	TY CLASSIFI	CATION AUTHORITY		3. DISTRIBUTION/AVAILABILITY OF REPORT			4 4 4 4 4 4 4 4 4	
26. DECLASSIFICATION/DOWNGRADING SCHEDULE		Approved for public release; distribution unlimited						
4. PERFOR	MING ORGAN	IZATION REPORT NUM	BER(S)	5. MONITORING ORGANIZATION REPORT NUMBER(S)				
	UBUF	FALO/DC/86/TR-2	7					
Depts	. Chemist	ng onganization cry & Physics ity of New York	6b. OFFICE SYMBOL (If applicable)	7a. NAME OF MONITORING ORGANIZATION				
Fronczak Hall, Amherst Campus Buffalo, New York 14260		75. ADDRESS (City, State and ZIP Code) Chemistry Program 800 N. Quincy Street Arlington, Virginia 22217						
ORGAN	IZATION	sponsoming 1 Research	8b. OFFICE SYMBOL (If applicable)	9. PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER  Contract N00014-86-K-0043				
8c. ADDRES	SS (City, State	and ZIP Code)	L	10. SOURCE OF FUR				
Chemi 800 N	stry Pro L. Quincy	gram		PROGRAM ELEMENT NO.	PROJECT NO.	TASK NO.	WORK UNIT	
11. TITLE		Role of Cohe	rences in the Re	elaxation of A	dsorbates	<del></del>		
12. PERSON	IAL AUTHOR	(\$)	Arnoldus and Tho			<del></del>		
134 TYPE	F REPORT	13b. TIME C		14. DATE OF REPOR				
16. SUPPLE	MENTARY NO		то	<u>December</u>	1986		28	
	Prepared for Publication in Physical Review B							
17 FIELD	COSATI		18 SUBJECT TERMS (C.	ontinue on reverse if ne			er)	
FIELD	GROUP	SUB. GR.	ADSORBATES  THERMAL RELAXAI	LEVEL WIDTHS TION DENSITY MATRIX			(	
10 10070	<b>27</b>		ROLE OF COHEREN		LIN	E PROFILES		
Adsorbed species on a solid-state surface interact with the large number of substrate modes, which gives rise to thermal relaxation. Commonly, the temporal evolution of the quantum state of the adsorbate is described by a master equation for the level populations (vibrational bond, internal modes, etc). It is pointed out that this approach does not decouple anymore from the time evolution of the coherences (off-diagonal matrix elements), which implies that a random-phase approximation cannot be justified, and that the density matrix of the adsorbate is not only determined by the Golden Rule transition constants. Especially the line profiles turn out to be very sensitive to the coherence-coherence couplings. Although the coherences vanish in thermal equilibrium, their time-regression operator, and hence their mitual couplings and their couplings to the populations, which determines the absorption profile, does not. This information is lost in a master-equation treatment of relaxation.								
20. DISTRIE	BUTION/AVA	LABILITY OF ABSTRAC	T	21. ABSTRACT SECU	JRITY CLASSIFI	CATION		
UNCLASSIFIED/UNLIMITED 🖾 SAME AS RPT. 🖾 DTIC USERS 🗆		Unclassified						
22a. NAME	OF RESPONS	BLE INDIVIDUAL		22b. TELEPHONE NUMBER (Include Area Code) 22c. OFFICE SYMBOL			MBOL	
Dr. David L. Nelson			(202) 696-44					

#### ROLE OF COHERENCES IN THE RELAXATION OF ADSORBATES

Henk F. Arnoldus and Thomas F. George

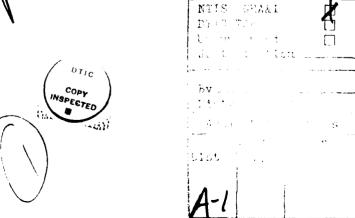
Departments of Physics & Astronomy and Chemistry 239 Fronczak Hall State University of New York at Buffalo Buffalo, New York 14260

#### **ABSTRACT**

Adsorbed species on a solid-state surface interact with the large number of substrate modes, which gives rise to thermal relaxation. Commonly, the temporal evolution of the quantum state of the adsorbate is described by a master equation for the level populations (vibrational bond, internal modes, etc). It is pointed out that this approach does not necessarily give a correct account of the coupling to the solid when the effective level-widths become comparable to the level separations, or larger. It is shown that the evolution of the populations does not decouple anymore from the time evolution of the coherences (off-diagonal matrix elements), which implies that a random-phase approximation cannot be justified, and that the density matrix of the adsorbate is not only determined by the Golden Rule transition constants. Especially the line profiles turn out to be very sensitive to the coherence-coherence couplings. Although the coherences vanish in thermal equilibrium, their time-regression operator, and hence their mutual couplings and their couplings to the populations, which determines the absorption profile, does not. This information is lost in a master-equation treatment of relaxation.

PACS: 71.36,78.90

property (seconder applicate absolutes comme presents contracts and applicates



Accession For

### I. INTRODUCTION

reviews, recessor reviews possesse weights reviews respect to seems appealed by the second

Coupling of adsorbed atoms or molecules on a surface to the degrees of freedom of the substrate, amounts to effective thermal relaxation of the internal molecular modes, or the vibrational bond with the solid. For molecules like CO on a metal surface, the excitation of internal stretching modes (vibrational levels) corresponds to a charge displacement, which couples to the motion of the electrons in the conduction band of the metal. Interaction of the electron cloud of the single molecule with the large number of electrons in the substrate then provides that the small system (the admolecule) is driven towards thermal equilibrium with the heat bath (the metal). This process is usually regarded as electron-hole pair formation in the metal. Another example of relaxation of adsorbates pertains to the kinetic coupling of an adatom in a vibrational (electromagnetic) bond with a crystal to the thermal motion of the surface atoms, which support the bond. In this fashion the kinetic and potential energy of an atom in an excited bound state on the surface, can be transferred into kinetic and potential energy of the crystal atoms. 3 Usually, this process is viewed as a phonon exchange between the adatom and the substrate. 4 Finally, we mention the irreversible dipole-coupling of dye molecules (coatings) on a dielectric to the surface-plasmon field. 5 This interaction is responsible for a dramatic change in the lifetime of the molecule, which in turn yields the celebrated phenomenon of enhanced Raman scattering, and surface-induced (Raman) resonances.

Commonly, the above-mentioned mechanisms for molecular relaxation, due to coupling with the substrate, are incorporated in the rate equations for the level populations  $n_i(t)$  (internal vibrational, kinetic or electronic) of the adparticle as  $^7$ 

$$\frac{d}{dt} n_{i}(t) = -\sum_{j} (n_{i}(t)a_{ij} - n_{j}(t)a_{ji}) + ... , \qquad (1.1)$$

where the transition constants  $a_{ij}$  are determined by the Golden Rule. Level  $|i\rangle$  decays to the other levels  $|j\rangle$  at a rate  $n_i a_{ij}$  (loss term), and gains population from transitions of levels  $|j\rangle$  to  $|i\rangle$  at a rate  $n_j a_{ji}$ . Balancing the contributions then gives the master equation (1.1), where the ellipsis denotes the remaining interactions with, for instance, a laser field. In a more thorough approach, which yields exactly the same result for the coupling with a heat bath, one starts with the full Schrödinger equation for the density operator  $\rho(t)$  of the solid, the adparticle and the interaction. With standard reservoir theory,  $p_i$  projection techniques  $p_i$  or a Langevin approach,  $p_i$  one then derives an equation of motion for the reduced density operator  $p_i$  of the adsorbate, defined as

$$\rho_0(t) = Tr_r \rho(t) , \qquad (1.2)$$

where  $\mathrm{Tr}_{\Gamma}$  indicates the partial trace over the reservoir states. Taking the diagonal part of the equation then results in the master equation (1.1) for the populations

$$n_{i}(t) = \langle i | \rho_{0}(t) | i \rangle$$
 (1.3)

If we consider the off-diagonal matrix elements (the coherences) of  $\rho_0(t),$  we obtain

$$\frac{d}{dt} \langle i | \rho_0(t) | j \rangle = \{ -i(\omega_i - \omega_j) - \frac{1}{2}(A_i + A_j) \} \langle i | \rho_0(t) | j \rangle + \dots, (1.4)$$

for i ≠ j, where

$$A_{i} = \sum_{j} a_{ij}$$
 (1.5)

equals the inverse lifetime of level  $|i\rangle$ , due to transitions to every other level  $|j\rangle$ , and  $\hbar\omega_i$  is the energy of  $|i\rangle$ . Hence any initial coherence  $\langle i|_{\mathcal{O}_0}(0)|_{j}\rangle$  vanishes exponentially on a time scale  $(\Lambda_i + \Lambda_j)^{-1}$  in the evolution to thermal equilibrium (long-time limit t  $+\infty$ , or steady state). In a random-phase approximation one omits the coherences from the beginning and considers only the time evolution of the populations. Since Eq. (1.4) for the coherences does not couple to the master equation (1.1) for the populations, this approach is justified by more elaborated theories.

However, this is not the whole story. First, the master equation does not embody the full dynamical behavior of the adparticle. It only provides information on the distribution of populations, the energy content of the molecule and the energy transfer into the solid. (Eq. (1.1) implies an equation for energy conservation, because a level at  $\hbar\omega_i$ , which is populated with  $n_i(t)$ , corresponds to an energy  $n_i\hbar\omega_i$  of the molecule.) Spectral information, like the line profiles for the absorption of radiation and the temporal correlations between the populations, which appear for instance in the response to a pulsed laser, are governed by the time regression of the coherences, rather than by the master equation. Therefore, in discarding Eq. (1.4) one loses valuable information on observable properties of the system.

Second, in the derivation of the master equation there is always the tacit assumption that the width of a specific transition  $|i\rangle + |j\rangle$ , which equals  $a_{ij}$ , is much smaller than the level separation  $|\omega_i - \omega_j|$ . Then one drops fast-oscillating terms with the Bohr frequencies  $\Delta_{ij} = \omega_i - \omega_j$ , with the argument that they will approximately average out to zero. This is a correct procedure if  $|\Delta_{ij}| >> a_{ij}$ . In general, however, it is not obvious that this condition is always satisfied. To be specific, for electron-hole

pair formation, both  $a_{ij}^{-1}$  and  $\Delta_{ij}^{-1}$  acquire values of the order of a picosecond, and for CO on copper, for instance, the inverse lifetime of the stretching modes exceeds the level separations. In the case of adsorption of atoms on a crystal, the timescales for relaxation typically range from nanoseconds to picoseconds. For weakly-bounded atoms (shallow potentials) the levels become closely spaced, and their separations can easily assume the order of magnitude of the damping constants.

In this paper we shall retain the couplings, which are due to the overlap of levels, and point out their significance. Especially the absorption profile for weak radiation appears to be sensitive to the coherence-coherence coupling, as will be illustrated by an example.

## II. RELAXATION THEORY

In order to display clearly the various approximations and to set the notation, we summarize the basic elements of relaxation theory in this section. With  $H_a$  the Hamiltonian of the adsorbate, which includes the binding energy to the surface (attractive force of electromagnetic origin), and  $H_r$  the substrate Hamiltonian, the equation of motion for the density operator  $\rho(t)$  of the active system reads

$$i\hbar \frac{d}{dt} \rho(t) = [H_a + H_r + SR, \rho(t)], \rho(t)^{\dagger} = \rho(t), Tr \rho(t) = 1$$
 (2.1)

Here the interaction between the molecule and the substrate, which gives rise to the relaxation, is divided as SR, where  $S = S^{\dagger}$  is a molecular operator (S = systems), and  $R = R^{\dagger}$  (reservoir) is an operator in the subspace of the solid. For instance, for coupling by single-phonon transitions, the operator S equals the derivative of the binding potential well, perpendicular to the surface, and R is the amplitude operator of an atom in the crystal. With a Taylor expansion it is always feasible to

factorize the interaction as  $\Sigma_i S_i R_i$ , but in order to avoid many obfuscating subscripts, we only retain a single term. In the case of phonon coupling, the subscript i indicates the number of phonons which are involved in a one-step transition. By writing SR for the interaction, we only keep track of single-phonon transition. This is already very accurate if the transition frequencies  $\Delta_{ij}$  are smaller than the Deybe frequency of the crystal, since then every pair of levels is resonantly couplied by a single-phonon interaction.

The standard integral of Eq. (2.1), which is suitable for the development of relaxation theory, is most conveniently derived with the aid of the interaction picture. With the Liouvillians

$$L_a = N^{-1}[H_a, \cdot] , L_r = N^{-1}[H_r, \cdot] ,$$
 (2.2)

we define the transformed density operator as

$$\sigma(t) = \exp(i(L_a + L_r)t) \rho(t) , \qquad (2.3)$$

which obeys the equation of motion

$$i h \frac{d}{dt} \sigma(t) = [S(t)R(t), \sigma(t)] . \qquad (2.4)$$

The free evolution of S and R is displayed in their time dependence, according to

$$S(t) = \exp(iL_a t)S , R(t) = \exp(iL_r t)R . \qquad (2.5)$$

Iterating Eq. (2.4) twice and differentiating the result with respect to time then yields the integral

$$i\frac{d}{dt}\sigma(t) = N^{-1}[S(t)R(t),\sigma(0)]$$

$$-iN^{-2} \int_{0}^{t} dt'[S(t)R(t),[S(t')R(t'),o(t')]] . \qquad (2.6)$$

As the initial value we can choose arbitrarily  $\sigma(0) = \sigma_0(0)\rho_{eq}$ , with  $\sigma_0(0) = Tr_r\sigma(0)$  the reduced density operator of the adsorbate and  $\rho_{eq}$  the thermal-equilibrium state of the solid. By definition,  $\rho_{eq}$  commutes with  $H_r$ , and we shall assume that

$$\operatorname{Tr}_{\mathbf{r}} \operatorname{R} \rho_{\mathbf{eq}} = 0 \quad . \tag{2.7}$$

This means that the interaction does not give rise to a net energy content of the molecule, which is exact in most cases. Otherwise the restriction (2.7) can be enforced by a proper transformation of  $\rho(t)$ , which shifts the interaction over its average. As a second step we write  $\sigma(t') = \sigma_0(t')\rho_{eq} + correction$ , which can always be done. After taking the trace in Eq. (2.6) over the reservoir states, we then obtain

$$\frac{d}{dt}\sigma_{0}(t) = -\frac{1}{2\pi} \int_{0}^{t} d\tau \{G(\tau)S(t)S(t-\tau)\sigma_{0}(t-\tau) + G(\tau)^{*}\sigma_{0}(t-\tau)S(t-\tau)S(t) - G(\tau)^{*}S(t)\sigma_{0}(t-\tau)S(t-\tau) - G(\tau)S(t-\tau)\sigma_{0}(t-\tau)S(t)\} + correction .$$
(2.8)

For later purposes we do not impose the condition  $\sigma_0^{\dagger} = \sigma_0$ , which would allow a contraction of terms. The interaction with the substrate is incorporated in the complex-valued reservoir correlation function

$$G(\tau) = 2\pi N^{-2} \operatorname{Tr}_{\mathbf{r}} R(\tau) R \rho_{\text{eq}} , \qquad (2.9)$$

which can be evaluated immediately for any prescribed R and  $H_{\rm r}$ . Among other features, this  $G(\tau)$  encompasses the temperature dependence of the coupling. Equation (2.8) is the usual starting point for reservoir theory.

A particularly transparent representation of Eq. (2.8) emerges if we adopt a Liouville-operator notation for the couplings in the integrand. To this end, we substitute  $S(t) = \exp(iL_a t)S$ , transform back to the p-picture, and define

$$L_{s} = [S, \cdot] \qquad (2.10)$$

Then Eq. (2.8) assumes the form

$$i\frac{d}{dt}\rho_{0}(t) = L_{a}\rho_{0}(t) - \frac{i}{2\pi}L_{S} \int_{0}^{t} d\tau \{G(\tau)e^{-iL_{a}\tau}(S\rho_{0}(t-\tau))\}$$

$$-G(\tau)^{*}e^{-iL_{a}\tau}(\rho_{0}(t-\tau)S)\} + correction . \qquad (2.11)$$

Next we introduce the correlation operator

$$L_{c}(\tau) = S \cdot G(\tau) - G(\tau)^{*} \cdot S , \qquad (2.12)$$

which enables to rewrite Eq. (2.11) compactly as

$$i\frac{d}{dt}\rho_0(t) = L_a\rho_0(t) - \frac{i}{2\pi} L_S \int_0^t d\tau e^{-iL_a\tau} L_c(\tau)\rho_0(t-\tau) + correction . \qquad (2.13)$$

As long as the correction terms are taken into consideration, and provided that condition (2.7) holds, this is still an exact integral of Eq. (2.1). Equation (2.13) clearly reveals the significance of  $L_{\rm C}(\tau)$ . It accounts for the memory in the interaction.

### III. RESERVOIR CONDITION

A solid has a broad, continuous spectrum of modes, which are coupled to the molecule by the SR interaction. This property assures that the correlation function  $G(\tau)$  from Eq. (2.9) decays to zero very fast for

increasing  $\tau$ . Typically, the time width of  $G(\tau)$  is of the order of the inverse cut-off frequency of the mode distribution, which is the Debye frequency for a harmonic crystal. Hence this time is much shorter than any time scale on which  $\sigma_0(t)$  varies, due to its coupling with the same continuum. If we indicate the correlation time of the reservoir by  $\tau_c$ , and the damping constant for the transition  $|i\rangle + |j\rangle$  by  $a_{ij}$ , as in Eq. (1.1), then the reservoir condition reads

$$a_{ij}^{\tau} < < 1$$
 (3.1)

for every i,j. For rare-gas atoms on a crystal like KCl, typical values of the product  $a_{ij}\tau_c$  range from 0.1 to 0.01. By definition, the value of the integral in Eq. (2.13) has an order of magnitude of  $a_{ij}$ , and it is easy to estimate that the correction terms are of the order of  $a_{ij}^2\tau_c$ . Therefore they can be discarded in comparison with  $a_{ij}$ . In the interaction picture,  $\sigma_0(t-\tau)$  evolves on a time scale  $a_{ij}^{-1}$ , which implies that we can replace  $\sigma_0(t-\tau)$  by  $\sigma_0(t)$  in Eq. (2.8). In the  $\rho$ -picture the density operator oscillates with the Bohr frequencies, and hence the corresponding approximation in Eq. (2.13) is  $^{14}$ 

$$\exp(iL_a(t-\tau))\rho_0(t-\tau) \simeq \exp(iL_at)\rho_0(t) . \qquad (3.2)$$

Then we can take  $\rho_0(t)$  outside the integral, and again with condition (3.1) we can replace the upper integration-limit by  $t = \infty$ . Combining everything then leads to the concise form of the equation of motion

$$i\frac{d}{dt} \rho_0(t) = (L_a - i\Gamma)\rho_0(t) . \qquad (3.3)$$

The Liouville operator  $\Gamma$  is defined by

$$\Gamma = \frac{1}{2\pi} L_s \int_0^\infty d\tau e^{-iL_a \tau} L_c(\tau) e^{iL_a \tau} , \qquad (3.4)$$

which accounts for the relaxation of the molecule, due to the coupling with the modes of the substrate. Recall that the only assumption in deriving Eq. (3.3) is the condition (3.1), which is fairly justified for adsorbates. Equations (3.3) and (3.4) constitute the full effect of the coupling to the substrate, including the time evolution of the coherences, coupling between coherences, level shifts, etc. The advantage of the Liouville approach, in contrast to a master-equation treatment, which relates matrix elements, is that the dynamics of the interaction is completely disentangled from the structure of the equation of motion, Eq. (3.3).

### IV. EVALUATION OF T

Equation (3.4) defines the relaxation operator  $\Gamma$  in terms of the Liouvillians  $L_a$  and  $L_c(\tau)$ . If we remember that

$$\exp(\pm iL_a\tau) \cdot = \exp(\pm iH_a\tau/\hbar) \cdot \exp(\mp iH_a\tau/\hbar) , \qquad (4.1)$$

and then insert the definition (2.12) of  $L_c(\tau)$  into Eq. (3.4), we find that  $\Gamma$  can alternatively be represented by

$$\Gamma = L_{\epsilon}(Q - Q^{\dagger}) , \qquad (4.2)$$

which involves the Hilbert-space operator

$$Q = \frac{1}{2\pi} \int_0^\infty d\tau G(\tau) e^{-iL_a \tau} S . \qquad (4.3)$$

Notice that Eq. (4.2) still contains four terms, because  $L_{_{\mathbf{S}}}$  is a commutator. This also immediately implies the properties

$$(\Gamma\sigma)^{\dagger} = \Gamma\sigma^{\dagger}$$
 ,  $Tr_a(\Gamma\sigma) = 0$  , (4.4)

for any  $\sigma$ . These relations are necessary for the conservation of Hermiticity and trace in the time evolution of  $\rho_0(t)$ .

Since  $L_a$  appears in an exponent in the definition of Q, an expansion in matrix elements is most convenient on a basis where  $L_a$  is diagonal, e.g., the adsorbate states  $|i\rangle$ . For simplicity we shall suppose that the states  $|i\rangle$  are non-degenerate. This is no restriction at all, but it avoids cumbersome notations. In terms of the projectors

$$P_{i} = |i\rangle\langle i| , \qquad (4.5)$$

the exponential in Eq. (4.3) can be expanded as

$$\exp(-iL_{a}\tau) \cdot = \sum_{ij} \exp(-i\Delta_{ij}\tau)P_{i} \cdot P_{j} . \qquad (4.6)$$

Then Q assumes the simple form

$$Q = \frac{1}{2} \sum_{ij} g_{ji} P_i SP_j , \qquad (4.7)$$

where the reservoir parameters  $\mathbf{g}_{ji}$  are defined by

$$g_{ji} = \frac{1}{\pi} \int_{0}^{\infty} d\tau \exp(-i\Delta_{ij}\tau)G(\tau) , \qquad (4.8)$$

which is essentially the Laplace transform of  $G(\tau)$ . Substituting Q and its Hermitian conjugate into Eq. (4.2) gives

$$\Gamma \sigma = \frac{1}{2} \sum_{ij} S_{ij} \{g_{ji} S | i > \langle j | \sigma - g_{ij}^{*} S \sigma | i > \langle j |$$

$$-g_{ji} | i > \langle j | \sigma S + g_{ij}^{*} \sigma | i > \langle j | S \} , \qquad (4.9)$$

which defines the action of  $\Gamma$  or an arbitrary Liouville vector  $\sigma$ . Here  $S_{ij}$  =  $\langle i | S | j \rangle$  is a matrix element of the molecular part of the interaction.

Equation (4.9) is a hybrid representation of  $\Gamma$ , since it contains matrix elements  $S_{ij}$ , as well as the operator S itself. With the closure relation

$$\sum_{i} P_{i} = 1 \quad , \tag{4.10}$$

we can cast Eq. (4.9) in the form

$$\Gamma \sigma = \frac{1}{2} \sum_{ijk} \{c_{kiij} | k \rangle \langle j | \sigma + c_{kiij}^{*} \sigma | j \rangle \langle k | \}$$

$$- \frac{1}{2} \sum_{ijk\ell} \{c_{k\ell ij}^{*} | i \rangle \langle j | \sigma | k \rangle \langle \ell | + c_{k\ell ij}^{*} | \ell \rangle \langle k | \sigma | j \rangle \langle i | \} , \qquad (4.11)$$

where we introduced the coefficients

$$c_{k\ell mn} = S_{k\ell} S_{mn} g_{nm} . \tag{4.12}$$

Hence the relaxation operator is determined by the reservoir parameters  $\mathbf{g}_{ij}$  and the matrix elements  $\mathbf{S}_{ij}$  between the wave functions  $|i\rangle$  and  $|j\rangle$  of the adsorbate. Both  $\mathbf{g}_{ij}$  and  $\mathbf{S}_{ij}$  can be evaluated directly, once the kind of substrate and the molecular wave functions (internal modes), or the binding potential (vibrational coupling to a crystal), are prescribed. 15

The relaxation gives rise to an effective width of the levels (their inverse lifetimes). If we assume that the overlap between different resonances is negligible, then we only have to retain couplings between pairs of levels in Eq. (4.11), rather than between four levels simultaneously. If we further neglect the imaginary part of  $g_{ij}$  (the level shifts), then Eq. (4.11) attains the familiar form  $^{16}$ 

$$\Gamma \sigma = \frac{1}{2} \sum_{ij} a_{ij} \{ P_i \sigma + \sigma P_i - 2P_j \langle i | \sigma | i \rangle \} , \qquad (4.13)$$

in terms of the rate constants  $a_{ij}$  for the transitions  $|i\rangle$  +  $|j\rangle$ 

$$a_{ij} = \text{Re } c_{k\ell\ell k} = |S_{k\ell}|^2 \text{Reg}_{k\ell} . \qquad (4.14)$$

It is easy to check that the simplified form (4.12) leads to the master equation (1.1).

## V. EQUATION OF MOTION

Numerical solution of the equation of motion (3.3) requires an expansion in matrix elements. With Eq. (4.11) for the relaxation, and

$$L_{a}\rho_{0} = \sum_{i} \omega_{i}(|i\rangle\langle i|\rho_{0} - \rho_{0}|i\rangle\langle i|) , \qquad (5.1)$$

for the free evolution, we obtain

$$\frac{d}{dt} \langle m | \rho_0 | n \rangle = -i \Delta_{mn} \langle m | \rho_0 | n \rangle - \frac{1}{2} \sum_{ij} \{ c_{miij} \langle j | \rho_0 | n \rangle + c_{niij} \langle m | \rho_0 | j \rangle \} 
+ \frac{1}{2} \sum_{ij} \{ c_{inmj} \langle j | \rho_0 | i \rangle + c_{imnj} \langle i | \rho_0 | j \rangle \} .$$
(5.2)

If we subsequently set m = n and use  $\rho_0^{\dagger} = \rho_0$ , we find

$$\frac{d}{dt} \langle m | \rho_0 | m \rangle = -\frac{1}{2} \sum_{ij} \{ c_{miij} \langle j | \rho_0 | m \rangle - c_{immj} \langle j | \rho_0 | i \rangle \}$$
+ Hermitian conjugate (5.3)

for the time derivative of the population  $\langle m|\rho_0|m\rangle$ . This result is by no means equivalent to the master equation (1.1). Even if we were to neglect the imaginary part of the coefficients, then the time evolution of the populations would still couple to the real part of the coherences  $\langle j|\rho_0|m\rangle$  ( $j \neq m$ ), due to overlapping resonances. Conversely, the time evolution of the coherences, as it follows from Eq. (5.2) with  $m \neq n$ , couples to the

populations and to every other coherence, in contrast to the simple exponential decay (Eq. (1.4)) in the limit of non-overlapping resonances. In conclusion, if the widths of transitions become comparable with the level separations, it is inevitable to take the coherences into consideration, which in turn prohibits the derivation of a genuine master equation. Stated otherwise, in this case a random-phase approximation cannot be justified.

## VI. STEADY STATE

Of particular importance is the long-time solution  $\overline{\rho}_0 = \rho_0(t \to \infty)$ . This steady-state density operator obeys  $d\overline{\rho}_0/dt = 0$ , and its matrix elements follow from Eqs. (5.2) and (5.3) with the left-hand sides replaced by zero. The relaxation of the reduced density operator to a steady state is a result of the coupling to the substrate. Apart from extravagent situations, this  $\overline{\rho}_0$  is unique. Therefore we can solve Eq. (5.3) by trial and error. If we assume that the coherences vanish in the steady state, e.g.

$$\langle i | \overline{\rho}_0 | j \rangle = \delta_{ij} \langle i | \overline{\rho}_0 | i \rangle = \delta_{ij} \overline{n}_i$$
, (6.1)

then Eq. (5.3) reduces to

$$\sum_{j} (\bar{n}_{i} a_{ij} - \bar{n}_{j} a_{ji}) = 0 , \sum_{i} \bar{n}_{i} = 1 , \qquad (6.2)$$

where the rate constants  $a_{ij}$  are defined in Eq. (4.14). This equation is exactly the same as Eq. (1.1) for  $t \to \infty$ , so with the left-hand side set equal to zero. Hence the long-time solution of the density matrix is diagonal, and determined by the Golden Rule transition-constants  $a_{ij}$ . Note that the imaginary parts of  $c_{k\ell\ell k}$  do not contribute. In terms of the solution  $\overline{n}_k$  of Eq. (6.2) and the projectors  $P_k$ , we can write  $\overline{\rho}_0$  as

$$\vec{\rho}_0 = \sum_{\mathbf{k}} \vec{n}_{\mathbf{k}} P_{\mathbf{k}} \quad , \tag{6.3}$$

which will be used in the next section.

Only in the transient region the coherences affect the details of the time evolution of the populations  $n_k(t)$ . Therefore it might appear that the importance of the coupling to the coherences, and in particular the coupling between different coherences, is marginal. Such is however not the case. Even in the steady state, where the coherences disappear identically, their time regression has a great significance for the calculation of observable quantities. It should be emphasized that, for instance, a level population is not directly accessible to experimental observation in general.

## VII. ABSORPTION PROFILE

A common method to observe resonances of adsorbates is by irradiation of the surface with a low-power monochromatic laser, and measuring the absorption as a function of the photon energy (frequency). Probing the system with a weak radiation field has the advantage that it does not disturb the molecule (excitation of internal modes), nor desorb the layer or heat the substrate. Furthermore, the intensity of the radiation (scattered or transmitted) can be detected with a high accuracy, partly due to the fact that only a relative measurment is required, which relates the absorption at a particular frequency to a calibrated off-resonance background level. Care should be exercised, however, in the interpretation of the spectrum. It is not the free molecule which absorbs the radiation, but the joint system of molecule, substrate and interaction. Conversely, this feature provides an interesting tool to investigate the molecule-surface interaction (binding potential, charge-exchange mechanism), or properties of the substrate (dispersion relations of phonons or polaritons). Especially for a transparent crystal, like for instance IR light on KCl, information about the crystal can be obtained by spectroscopic methods in this way, which is

not feasible without the coating. The adbond-mediated absorption profile will reflect the details of the coupling mechanism of the molecule to the substrate, and the properties of the solid itself. We remark that even if both the adsorbate and the substrate are transparent for a particular frequency, the bond can be optically active. This is for instance the case for rare-gas atoms on an alkali-chloride crystal. Then the absorption profile will reveal the properties of the wave function of the vibrational state, and as we show below, in great detail.

If we indicate by  $\underline{\mu}$  the dipole-moment operator of the molecule or the bond (or both), and by  $\underline{\varepsilon}$  the polarization of the probe beam, then the absorption profile is determined by the time regression of the operator

$$d = \mu \cdot \varepsilon \qquad (7.1)$$

With d(t) the Heisenberg representation of d, the number of absorbed photons per unit of time from the incident field with frequency  $\omega$  equals  $^{17}$ 

$$I(\omega) = I_{p}(\varepsilon_{0}N^{2}c)^{-1}Re \int_{0}^{\infty} dt \ e^{i\omega t} \ Tr \ \overline{\rho}[d(t)^{\dagger}, d] , \qquad (7.2)$$

where  $I_p$  is the laser power (energy per unit of time through a unit area, perpendicular to the direction of propagation). Multiplication of  $I(\omega)$  by  $\hbar\omega$  gives the absorbed energy per unit of time. Here,  $\bar{\rho}$  is the thermal-equilibrium state of the entire system, and the time regression of d(t) is governed by the Hamiltonian  $H_a$  +  $H_r$  + SR from Eq. (2.1).

After a transformation to the Schrödinger picture, we can eliminate the reservoir degrees of freedom from the integrand in Eq. (7.2) along exactly the same lines as we derived Eq. (3.3) for the reduced density operator  $\rho_{\Omega}(t)$ . We obtain

$$\operatorname{Tr}\bar{\rho}[d(t)^{\dagger},d] = \operatorname{Tr}_{a}d^{\dagger}e^{-i(L_{a}^{-i\Gamma})t}[d,\bar{\rho}_{0}]$$
, (7.3)

where  $T_a$  runs over the adsorbate states only. Equation (7.3) can be regarded as Liouville-operator representation of the quantum-regression theorem. <sup>18</sup> Then we insert Eq. (7.3) into Eq. (7.2) and perform the time integration, which yields the representation

$$I(\omega) = I_{p}(\epsilon_{0} h^{2}c)^{-1} ReTr_{a} d^{\dagger} \frac{i}{\omega - L_{a} + i\Gamma} [d, \bar{\rho}_{0}]$$
 (7.4)

in terms of an operator inversion. The upper limit  $t = \infty$  does not contribute, due to the identity

$$-i(L_a - i\Gamma)t$$

$$\lim_{t \to \infty} e \qquad [d, \overline{\rho}_0] = \overline{\rho}_0 \operatorname{Tr}_a[d, \overline{\rho}_0] = 0 , \qquad (7.5)$$

which in turn follows from the facts that  $\overline{\rho}_{\Omega}$  is the solution of

$$(L_a - i\Gamma)\bar{\rho}_0 = 0 \tag{7.6}$$

and that the trace is conserved in a time regression with  $\exp(-i(L_a-i\Gamma)t)$ . We recall that the commutator  $[d,\bar{\rho}_0]$  gives rise to the terms  $d\bar{\rho}_0$  and  $\bar{\rho}_0d$ , which correspond to stimulated absorption and emission in the laser mode respectively. The profile  $I(\omega)$  is the balance between these two processes.

Since we suppress the degeneracies of the levels, we can expand the operator d on the adsorbated states as

$$d = \sum_{i,j} d_{i,j} |i\rangle\langle j| . \qquad (7.7)$$

With the representation (6.3) of the steady-state solution, we find

$$[\mathbf{d}, \bar{\rho}_0] = \sum_{i,j} (\bar{\mathbf{n}}_j - \bar{\mathbf{n}}_i) \mathbf{d}_{i,j} | i \rangle \langle j | . \qquad (7.8)$$

Substitution into Eq. (7.4), expanding  $d^{\dagger}$  as in Eq. (7.7), and taking the trace then gives

$$I(\omega) = I_{p}(\epsilon_{0}N^{2}c)^{-1} \sum_{ijk\ell} (\bar{n}_{j} - \bar{n}_{i}) \operatorname{Re} d_{ij}d_{k\ell}^{*} \langle k | (\frac{i}{\omega - L_{a} + i\Gamma} | i \rangle \langle j |) | \ell \rangle .$$
(7.9)

The matrix elements of  $\omega$  -  $L_a$  + if can be read off immediately from Eq. (5.2), and after inversion of this matrix, Eq. (7.9) yields the absorption profile. Hence for a system of N levels, the evaluation of  $I(\omega)$  requires only the inversion of an  $N^2 \times N^2$  matrix.

From the explicit representation (7.9) it follows that  $I(\omega)$  is determined by the time regression of the coherence  $|i\rangle\langle j|$ ,  $(i\neq j)$ . In the time domain, like in Eq. (7.1), we propagate  $|i\rangle\langle j|$  with  $\exp(-i(L_a-i\Gamma)t)$ , and then take the coherence  $\langle k|\dots|\ell\rangle$  of the result at time t. A Fourier transform then gives the spectral profile. This elucidates the importance of the coherences in the observation of adsorbates with spectroscopic methods. It is their time regression which determines the spectral distribution, whereas the populations only appear as an overall factor  $\bar{n}_j$  -  $\bar{n}_i$ . Furthermore, the spectral resolution involves the complete operator  $L_a$  -  $i\Gamma$ , which represents the free evolution of the molecule, the damping, the level shifts, and all the couplings between coherences and populations.

In the secular approximation, Eq. (4.13), where only couplings between pairs of levels are taken into account, only the terms with i = k,  $j = \ell$  survive in Eq. (7.9). We notice that for  $(i,j) \neq (k,\ell)$  an overall factor  $d_{ij}d_{k\ell}$  arises, rather than  $|d_{ij}|^2$ . This product of matrix elements carries information on the relative phases of the dipole-moment matrix elements  $d_{ij}$ , which is not the case in the secular limit, where only  $|d_{ij}|^2$  appears. Therefore, for transitions which have a sufficient overlap, it should be feasible to extract their relative phase from an absorption measurement.

### VIII. TWO-LEVEL SYSTEM

In order to display the significance of the various notions, we utilize the two-level system. For the case of a vibrational coupling of an atom to a crystal, this situation can occur if the potential well is shallow enough, so that it supports only two discrete levels. The steady-state populations are readily found from Eq. (6.2). We obtain

$$\bar{n}_1 = \frac{a_{21}}{a_{21} + a_{12}}$$
 ,  $\bar{n}_2 = \frac{a_{12}}{a_{21} + a_{12}}$  . (8.1)

Next we neglect the self-coupling of a level, which means that we assume  $S_{11} = S_{22} = 0$ . The equation for the coherence  $\rho_{21}(t)$  follows from Eq. (5.2). Explicitly

$$\frac{d}{dt} \rho_{21}(t) = -i \Delta_{21} \rho_{21}(t) - \frac{1}{2} (c_{2112} + c_{1221}^*) \rho_{21}(t) + \frac{1}{2} (c_{2121} + c_{1212}^*) \rho_{12}(t) , \qquad (8.2)$$

and the equation for  $\rho_{12}(t) = \rho_{21}(t)^*$  follows after a complex conjugation. We shall write  $\Delta_{21} = \omega_0$  for the resonance frequency of the adsorbate, before coupling to the reservoir, and we introduce the notations

$$\eta = \frac{1}{2} |S_{21}|^2 (g_{21} + g_{12}^*) , \qquad (8.3)$$

$$S_{21} = |S_{21}| \exp(i\phi)$$
, (8.4)

where the latter defines the phases  $\phi$  of  $S_{21}$ . Then Eq. (8.2) attains the form

$$\frac{d}{dt}\rho_{21}(t) = -(i\omega_0 + \eta)\rho_{21}(t) + \eta^* \exp(2i\phi)\rho_{12}(t), \qquad (8.5)$$

which shows immediately that  $\bar{\rho}_{21} = \bar{\rho}_{12} = 0$ , in agreement with Eq. (6.1). The second term on the right-hand side represents a coupling between the

coherences  $\rho_{21}(t)$  and  $\rho_{12}(t)$ . This term would be discarded in a secular approximation.

Equation (8.5) together with its complex conjugate constitutes a closed set, which has the characteristic frequencies

$$\omega_{\pm} = \pm \{\omega_0(\omega_0 + i(\eta^* - \eta)) - \frac{1}{4}(a_{21} + a_{12})^2\}^{\frac{1}{2}} - \frac{1}{2}i(a_{21} + a_{12}), \quad (8.6)$$

where we used

$$\eta + \eta^* = a_{21} + a_{12}$$
 (8.7)

In the secular limit  $\omega_0 >> a_{21} + a_{12}$ , they reduce to  $\omega_{\pm} = \pm \omega_0 - \frac{1}{2}i(a_{21} + a_{12})$ , and hence the resonance is situated at  $\omega_0$  with a width equal to  $\frac{1}{2}(a_{21} + a_{12})$ . Conversely, for  $a_{21} + a_{12} >> \omega_0$  we find  $\omega_{\pm} = 0$ ,  $\omega_{\pm} = -i(a_{21} + a_{12})$ , which are both situated at  $\omega_0 = 0$ .

The full absorption profile  $I(\omega)$ , Eq. (7.9), is determined by the Liouville operator  $\omega$  -  $L_a$  + i $\Gamma$ . From Eq. (5.2) we can easily construct a matrix representation for -i( $L_a$  - i $\Gamma$ ), which in turn gives

$$\omega - L_{a} + i\Gamma = \begin{bmatrix} \omega + ia_{21} & -ia_{12} & 0 & 0 \\ -ia_{21} & \omega + ia_{12} & 0 & 0 \\ 0 & 0 & \omega - \omega_{0} + i\eta & -i\eta \exp(2i\phi) \\ 0 & 0 & -i\eta \exp(-2i\phi) & \omega + \omega_{0} + i\eta \end{bmatrix}$$
(8.8)

on the basis  $|2\rangle\langle2|$ ,  $|1\rangle\langle1|$ ,  $|2\rangle\langle1|$ ,  $|1\rangle\langle2|$ . Inversion of this matrix and substitution into Eq. (7.9) then readily yields

$$I(\omega) = BI_{p} \frac{a_{21} - a_{12}}{a_{21} + a_{12}} \frac{1}{\pi} Re \frac{2i\omega_{0}}{(\omega + \omega_{0} + i\eta^{*})(\omega - \omega_{0} + i\eta) + \eta\eta^{*}}, \quad (8.9)$$

where we introduced the Einstein B-coefficient

$$B = \frac{\pi}{\epsilon_0 N^2 c} |\mu_{21} \cdot \epsilon|^2 , \qquad (8.10)$$

pertaining to stimulated transitions between  $|1\rangle$  and  $|2\rangle$ . Notice that the phase  $\phi$  of  $S_{21}$  disappears from  $I(\omega)$ , as could be anticipated. Only relative phase differences between wave functions of pairs of levels might have a significance, and hence the phase difference  $\phi$ , related to the wave functions of a two-state system, should vanish in observable quantities. The resonances of  $I(\omega)$  are situated at the real parts of the zero's  $\omega_{\pm}$  of the denominator. Since  $Re \omega_{+} = -Re\omega_{-}$  there is only a single peak in  $I(\omega)$  for positive frequencies  $\omega$ .

In the secular limit we can omit the term  $\eta\eta^{\star}$  in the denominator (with respect to  $\omega_{\Omega}^{~2}),$  and then the profile reduces to

$$I(\omega)_{s} = BI_{p} \frac{a_{21} - a_{12}}{a_{21} + a_{12}} \frac{1}{\pi} Re_{\omega - \omega_{0} + i\eta}$$
, (8.11)

which is a Lorentzian around  $\omega_0$  + Im $\eta$ , with a half width at half maximum equal to Re  $\eta = \frac{1}{2}(a_{21} + a_{12})$ . In Figs. 1 and 2 we have plotted  $I(\omega)$  and  $I(\omega)_s$  for Im  $\eta = 0$  and for different values of Re  $\eta$ . Note that  $I(\omega)$  and  $I(\omega)_s$  assume the same value at the transition frequency  $\omega_0$ , if Im  $\eta = 0$ . Increasing Re  $\eta$  shifts the peak in  $I(\omega)$  towards lower frequencies, without a significant broadening. On the other hand, an increas of Re $\eta$  in  $I(\omega)_s$  broadens the line, without shifting it. The qualitative different effects on  $I(\omega)_s$ , as compared to the approximation  $I(\omega)_s$ , arise purely due to the inclusion of the coherence-coherence coupling. The shift of the line in  $I(\omega)_s$  should not be confused with the shift Im  $\eta$  (Lamb shift), which is always present but, in general, small. Shifts and widths of absorption lines are directly amenable to experimental observation, and hence a verification of these predictions should be feasible.

### IX. CONCLUSIONS

Coherences play a pronounced role in the relaxation of adsorbates if the widths of the transitions (relaxation constants) become comparable to or exceed the level separations. In the transient region the time evolution of the populations of the adsorbate states couples to the evolution of the coherences, which prohibits a description in terms of a master equation. For  $t \rightarrow \infty$  (steady state, thermal equilibrium) the coherences vanish, and a time-independent master equation emerges, which contains the Golden-Rule transition constants as parameters. Measurable quantities which are determined by a two-time quantum expectation value, like correlation functions or spectrally-resolved properties, however, involve the timeevolution operator  $L_a$  -  $i\Gamma$  for the density matrix  $\rho_{\Omega}(t).$  This includes all couplings between populations and coherences, and between coherences among each other. Even in the steady state, where the coherences disappear, their time-regression operator obviously does not. Therefore, a correct evaluation of steady-state properties requires that the coupling with coherences is retained. In other words, a random-phase or secular approximation is not exact in general.

We have applied a Liouville-operator formalism to derive a condensed form, Eq. (3.3), of the equation of motion for the reduced density operator  $\rho_0(t)$  of the adsorbate. After some algebraic manipulations, and an expansion in matrix elements, we arrived at Eq. (5.2), which generalizes the master equation (1.1). It should be stressed that Eq. (5.2) contains the same parameters as Eq. (1.1), so that no additional information about the system is required. Only the coupling between the different matrix elements is more complicated. Discarding various non-secular couplings yields again Eq. (1.1).

Subsequently we have considered the probe-absorption spectrum  $I(\omega)$ , which was expressed in the resolvent  $(\omega - L_a + i\Gamma)^{-1}$  in Eq. (7.9). With a two-level example it has been illustrated how the formal expression can be evaluated, and what the relevance of the coherence-coherence coupling can be for the spectral distribution. The results have been compared with the secular approximation, where  $I(\omega)$  is a Lorentzian.

### **ACKNOWLEDGMENTS**

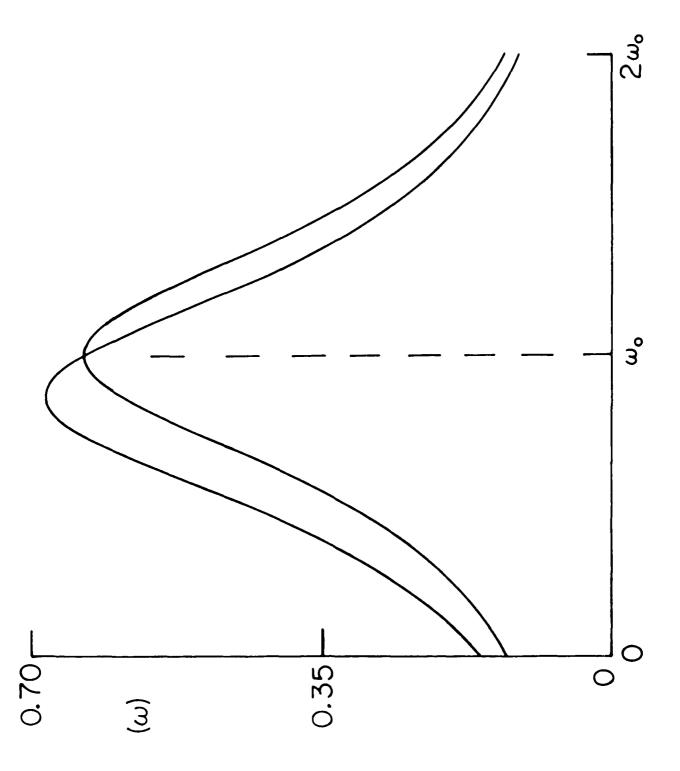
This research was supported by the Office of Naval Research, the Air Force Office of Scientific Research (AFOSR) United States Air Force, under Contract No. F49620-86-C-0009, and the National Science Foundation under Grant CHE-8519053.

#### REFERENCES

- 1. A. Peremans, J. Darville, J. M. Gilles and T. F. George, Phys. Rev. B, submitted.
- 2. B. N. J. Persson and M. Persson, Solid State Commun. 36, 175 (1980).
- 3. S. Efrima, C. Jedrzejek, K. F. Freed, E. Hood and H. Metiu, J. Chem. Phys. 79, 2436 (1983).
- 4. H. F. Arnoldus, S. van Smaalen and T. F. George, Phys. Rev. B <u>34</u>, 6902 (1986).
- 5. M. R. Philpott, J. Chem. Phys. 62, 1812 (1975).
- 6. G. S. Agarwal, Phys, Rev. A 12, 1475 (1975).
- 7. 2. W. Gortel, H. J. Kreuzer, R. Teshima and L. A. Turski, Phys. Rev. B <u>24</u>, 4456 (1981).
- 8. G. Korzeniewski, E. Hood and H. Metiu, J. Vac. Sci. Technol. <u>20</u>, 594 (1982).
- W. H. Louisell, Quantum Statistical Properties of Radiation (Wiley, New York, 1973).
- 10. R. W. Zwanzig, in Lectures in Theoretical Physics, edited by W. E. Britten, B. Downs and J. Downs (Interscience, New York, 1961), Vol. III, P. 106 ff.
- 11. H. F. Arnoldus and T. F. George, J. Opt. Soc. Am. B (1987) in press.
- 12. We adopt a Liouville notation (super operator representation), which allows a more concise formulation of the theory, as given by C. Cohen-Tannoudji, in Frontiers in Laser Spectroscopy, Proceedings of the 27th Les Houches Summer School, edited by R. Balian, S. Haroche and S. Liberman (North-Holland, Amsterdam, 1977).
- Z. W. Gortel, H. J. Kreuzer, P. Piercy and R. Teshima, Phys. Rev. B <u>27</u>, 5066 (1983).
- 14. J. R. Ackerhalt and J. H. Eberly, Phys. Rev. D 10, 3350 (1974).
- 15. Analytical expressions for the case of a Morse potential are given in Ref. 3.
- 16. G. S. Agarwal, in Springer Tracts in Modern Physics, edited by G. Hohler et al. (Springer-Verlag, New York, 1974), Vol. 70.
- 17. G. Nienhuis, Physica <u>66</u>, 245 (1973).
- 18. M. Lax, Phys Rev. 172, 350 (1968).

### **CAPTIONS**

- Fig. 1. Absorption profile  $I(\omega)$  from Eq. (8.9) as a function of  $\omega$ . The overall factor  $BI_p(a_{21}-a_{12})/(a_{21}+a_{12})^{-1}$  is to entropy the unity. Frequencies are in units of  $\omega_0$ , and the relaxation constant equals  $\eta=0.5$ . The profile which is symmetric around  $\omega_0$  is the secular approximation  $I(\omega)_s$  from Eq. (8.11).
- Fig. 2. Same as Fig. 1. but with  $\eta$  = 1.5. In this case the width of the transition is larger than the level separation, and it is seen that the resonance at  $\omega_0$  vanishes completely. The combined system of adsorbate and substrate gives rise to a resonance near  $\omega$  = 0, which is not found in the secular limit. There the peak at  $\omega_0$  is smeared out to form a continuous background. This exhibits clearly the significance of the non-secular couplings if the levels have overlapping resonances.



France 1

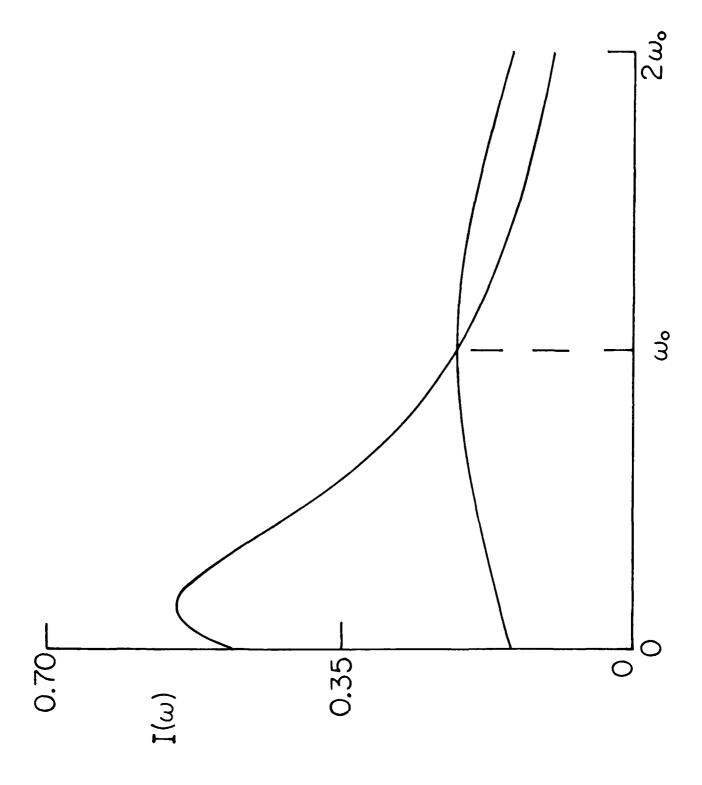


Figure 2

Secondarional account defended because besides resident account

# 01/1113/86/2

である。1911年のできたがない。 日本ではないない。1918年のできたがは、日本のののでは、1918年のできた。1918年のできた。1918年の191

# TECHNICAL REPORT DISTRIBUTION LIST, GEN

	No. Copies		No. Copies
Office of Naval Research Attn: Code 1113 800 N. Quincy Street Arlington, Virginia 22217-5000	2	Dr. David Young Code 334 NORDA NSTL, Mississippi 39529	1
Dr. Bernard Douda Naval Weapons Support Center Code 50C Crane, Indiana 47522-5050	1	Naval Weapons Center Attn: Dr. Ron Atkins Chemistry Division China Lake, California 93555	1
Naval Civil Engineering Laboratory Attn: Dr. R. W. Drisko, Code L52 Port Hueneme, California 93401	1	Scientific Advisor Commandant of the Marine Corps Code RD-1 Washington, D.C. 20380	1
Defense Technical Information Center Building 5, Cameron Station Alexandria, Virginia 22314	12 high quality	U.S. Army Research Office Attn: CRD-AA-IP P.O. Box 12211 Research Triangle Park, NC 27709	1
DTNSRDC Attn: Dr. H. Singerman Applied Chemistry Division Annapolic, Maryland 21401	1	Mr. John Boyle Materials Branch Naval Ship Engineering Center Philadelphia, Pennsylvania 19112	
Dr. William Tolles Superintendent Chemistry Division, Code 6100 Naval Research Laboratory	1	Naval Ocean Systems Center Attn: Dr. S. Yamamoto Marine Sciences Division San Diego, California 91232	1
Washington, D.C. 20375-5000	. •	Dr. David L. Nelson Chemistry Division Office of Naval Research 800 North Quincy Street Arlington, Virginia 22217	1

Dr. J. E. Jensen Hughes Research Laboratory 3011 Malibu Canyon Road Malibu, California 90265

Dr. J. H. Weaver
Department of Chemical Engineering
and Materials Science
University of Minnesota
Minneapolis, Minnesota 55455

Dr. A. Reisman Microelectronics Center of North Carolina Research Triangle Park, North Carolina 27709

Dr. M. Grunze Laboratory for Surface Science and Technology University of Maine Orono, Maine 04469

Dr. J. Butler Naval Research Laboratory Code 6115 Washington D.C. 20375-5000

Dr. L. Interante Chemistry Department Rensselaer Polytechnic Institute Troy, New York 12181

Dr. Irvin Heard Chemistry and Physics Department Lincoln University Lincoln University, Pennsylvania 19352

Dr. K.J. Klaubunde Department of Chemistry Kansas State University Manhattan, Kansas 66506 Dr. C. B. Harris Department of Chemistry University of California Berkeley, California 94720

Dr. F. Kutzler
Department of Chemistry
Box 5055
Tennessee Technological University
Cookesville, Tennessee 38501

Dr. D. Dilella Chemistry Department George Washington University Washington D.C. 20052

Dr. R. Reeves Chemistry Department Renssaeler Polytechnic Institute Troy, New York 12181

Dr. Steven M. George Stanford University Department of Chemistry Stanford, CA 94305

Dr. Mark Johnson Yale University Department of Chemistry New Haven, CT 06511-8118

Dr. W. Knauer Hughes Research Laboratory 3011 Malibu Canyon Road Malibu, California 90265

Or. G. A. Somorjai Department of Chemistry University of California Berkeley, California 94720

Dr. J. Murday Naval Research Laboratory Code 6170 Washington, D.C. 20375-5000

Dr. J. B. Hudson Materials Division Rensselaer Polytechnic Institute Troy, New York 12181

Dr. Theodore E. Madey Surface Chemistry Section Department of Commerce National Bureau of Standards Washington, D.C. 20234

Dr. J. E. Demuth
IBM Corporation
Thomas J. Watson Research Center
P.O. Box 218
Yorktown Heights, New York 10598

Dr. M. G. Lagally
Department of Metallurgical
and Mining Engineering
University of Wisconsin
Madison, Wisconsin 53706

Dr. R. P. Van Duyne Chemistry Department Northwestern University Evanston, Illinois 60637

Dr. J. M. White Department of Chemistry University of Texas Austin, Texas 78712

Dr. D. E. Harrison Department of Physics Naval Postgraduate School Monterey, California 93940 Dr. R. L. Park
Director, Center of Materials
Research
University of Maryland
College Park, Maryland 20742

Dr. W. T. Peria Electrical Engineering Department University of Minnesota Minneapolis, Minnesota 55455

Or. Keith H. Johnson
Department of Metallurgy and
Materials Science
Massachusetts Institute of Technology
Cambridge, Massachusetts 02139

Dr. S. Sibener
Department of Chemistry
James Franck Institute
5640 Ellis Avenue
Chicago, Illinois 60637

Dr. Arnold Green Quantum Surface Dynamics Branch Code 3817 Naval Weapons Center China Lake, California 93555

Dr. A. Wold Department of Chemistry Brown University Providence, Rhode Island 02912

Dr. S. L. Bernasek Department of Chemistry Princeton University Princeton, New Jersey 08544

Dr. W. Kohn Department of Physics University of California, San Diego La Jolla, California 92037 ogstaccountercounter (passaca)

Or. F. Carter Code 6170 Naval Research Laboratory Washington, D.C. 20375-5000

Dr. Richard Colton Code 6170 Naval Research Laboratory Washington, D.C. 20375-5000

Dr. Dan Pierce National Bureau of Standards Optical Physics Division Washington, D.C. 20234

Dr. R. Stanley Williams
Department of Chemistry
University of California
Los Angeles, California 90024

Dr. R. P. Messmer Materials Characterization Lab. General Electric Company Schenectady, New York 22217

Dr. Robert Gomer
Department of Chemistry
James Franck Institute
5640 Ellis Avenue
Chicago, Illinois 60637

Dr. Ronald Lee R301 Naval Surface Weapons Center White Oak Silver Spring, Maryland 20910

Dr. Paul Schoen Code 6190 Naval Research Laboratory Washington, D.C. 20375-5000 Dr. John T. Yates Department of Chemistry University of Pittsburgh Pittsburgh, Pennsylvania 15260

Dr. Richard Greene Code 5230 Naval Research Laboratory Washington, D.C. 20375-5000

Dr. L. Kesmodel
Department of Physics
Indiana University
Bloomington, Indiana 47403

Dr. K. C. Janda University of Pittsburg Chemistry Building Pittsburg, PA 15260

Dr. E. A. Irene
Department of Chemistry
University of North Carolina
Chapel Hill, North Carolina 27514

Dr. Adam Heller Bell Laboratories Murray Hill, New Jersey 07974

Dr. Martin Fleischmann Department of Chemistry University of Southampton Southampton 509 5NH UNITED KINGDOM

Dr. H. Tachikawa Chemistry Department Jackson State University Jackson, Mississippi 39217

Dr. John W. Wilkins Cornell University Laboratory of Atomic and Solid State Physics Ithaca, New York 14853

Dr. R. G. Wallis Department of Physics University of California Irvine, California 92664

Dr. D. Ramaker Chemistry Department George Washington University Washington, D.C. 20052

Dr. J. C. Hemminger . Chemistry Department University of California Irvine, California 92717

Dr. T. F. George Chemistry Department University of Rochester Rochester, New York 14627

Dr. G. Rubloff IBM Thomas J. Watson Research Center P.O. Box 218 Yorktown Heights, New York 10598

Dr. Horia Metiu Chemistry Department University of California Santa Barbara, California 93106

and apprecial laterature personal consister property leavester manner

Dr. W. Goddard
Department of Chemistry and Chemical
Engineering
California Institute of Technology
Pasadena, California 91125

Dr. P. Hansma Department of Physics University of California Santa Barbara, California 93106

Dr. J. Baldeschwieler
Department of Chemistry and
Chemical Engineering
California Institute of Technology
Pasadena, California 91125

Dr. J. T. Keiser Department of Chemistry University of Richmond Richmond, Virginia 23173

Or. R. W. Plummer
Department of Physics
University of Pennsylvania
Philadelphia, Pennsylvania 19104

Dr. E. Yeager Department of Chemistry Case Western Reserve University Cleveland, Ohio 41106

Dr. N. Winograd
Department of Chemistry
Pennsylvania State University
University Park, Pennsylvania 16802

Dr. Roald Hoffmann Department of Chemistry Cornell University Ithaca, New York 14853

Dr. A. Steckl
Department of Electrical and
Systems Engineering
Rensselaer Polytechnic Institute
Troy, NewYork 12181

Dr. G.H. Morrison Department of Chemistry Cornell University Ithaca, New York 14853

DT/C